# PARAMETRIC INVESTIGATION TO OPTIMIZE THE DYNAMIC RANGE OF MR DAMPER FOR VIBRATION CONTROL

BY

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### ABSTRACT

This research sought to identify the solution of shock absorption for vibration control (in this case, to reduce the effect of the heel strike of the transtibial amputee in walking). This research proposes a device which is a damper-based shock absorber installing on a prosthetic limb that will be used by the transtibial amputee. The prosthetic leg adopts a semi-active damper to capture the advantages of passive damper along with to perform as good as an active damper. Magnetorheological (MR) damper, which utilizes the benefits of MR fluids, is one of the most promising semi-active devices in mitigating the vibration. MR fluids is a smart material because of the ability to control the rheological properties by tuning the external magnetic field strength. Moreover, mechanical simplicity, fast response, and low power consumption have attracted more interest on this damper. However, the challenging aspect of utilizing this device is to understand their performance under varied input parameters. Understanding the behavior of the MR damper is the critical feature to use this damper fully. A well-known mathematical model, the Phenomenological (Modified Bouc-Wen) model, is used to model the MR damper behavior. To use this model, a relationship between the damper parameters, including force, displacement, velocity, current, and frequency, should be available. An experimental study of MR damper is done by the researcher to acquire those relationships. A comprehensive optimization methodology to estimate the parameters of the Modified Bouc-Wen model is necessary. The researcher compares two optimization algorithm, which is Particle Swarm Optimization (PSO) and Genetic Algorithm (GA) to estimate the parameters. From the comparison, PSO, inspired by the behavior of bees swarming for the optimization methods, has higher accuracy, which is 95.92% compared to GA, which is 94.71%. The precision of the optimization of the Modified Bouc-Wen parameters is from 92.3% to 96.5%. Each parameter fits the function of input current and frequency using the polynomial equation (maximum 3rd polynomial order). The precision of the fitting is from 87% to 98.4%. Robust Controller is developed to control the MR damper for transtibial prosthetic limbs. In this research, prosthetic limb applications adapt H∞ robust controller and inverse MR damper model. The result of the controller design compared to the targeted behavior is up to 92.51% accuracy. The simulation's performance is presumed to be acceptable since it almost followed the pattern of the targeted design.

### ملخص البحث

هذا البحث سعى إلى تحديد حل امتصاص الصدمات للتحكم في الاهتزاز ( في هذه الحالة، لتقليل تأثير ضربة الكعب للبتر العضلي أثناء المشى). يقترح هذا البحث على جهاز قائم على المخمد لامتصاص الصدمات والتي يتم تركيبها على طرف صناعي يتم استخدامه بواسطة العضو المبتور. تعتمد الساق الصناعية على مخمد نصف نشط لالتقاط المز ايا المخمد سلبي كاداء جيدة مثل المخمد النشط. MR) Magnetorheological) التي تستخدم فوائد سوائل الرنين المغناطيسي،وتعتبر هي أحد أكثر الأجهزة الواعدة شبه النشطة في تخفيف الاهتزاز. موائع MR مادة ذكية لأن قدرتها في التحكم على خصائص الروماتيزم بضبط قوة المغناطيسي الخارجي. بالاضافة إلى ذلك، البساطة الميكانيكية والاستجابة السريعة وانخفاض استهلاك للطاقة عمل جذب مهم لهذا المخمد. ومع ذلك، فان أشد جوانب التحدي في استخدام هذا الجهاز هو فهم أدائها عند تغير بعض المدخلات. إن فهم سلوك MR المخمد هي الميزة الأساسية لاستخدام هذا المخمد بالكامل. و المعرفة الكاملة بالنمودج الرياضي معروف وهو نموذج (Modified-Bouc-Wen) يُستخدم هذا النمودج لمعالجة سلوك المخمد MR. لاستخدام هذا النموذج، يجب أن تتوفر علاقة بين معاملات المخمد، بما في ذلك القوة والازاحة والسرعة والتيار والتردد. يتم إجراء دراسة تجريبية لمخمد MR من الباحث لاكتساب تلك العلاقات. ومنهج التحسين الشامل أمر ضروري. في تقدير معلمات نموذج Bouc-Wen المعدل. ويقارن الباحث بين خوارز ميتين المحسنتين المحسنتين Particle Swarm Optimization (PSO) وخوارزمية الجينية (GA) لتقدير المعاملات. ومن خلال المقارنة، PSO، مستوحاة من سلوك احتشاد النحل لأسلوب التحسين، لذلك لديه الدقة أعلى وهي %95.92 مقارنة بGA وهي 94.71%. ودقة التحسين من Bouc-Wen معدل المعلمة وهي من %92.3 إلى %96.5. ويناسب كل معامل وظيفة إدخال التيار والتردد باستخدام معادلة متعددة الحدود (أكثر معادلة متعددة الحدود الثالث). ودقة الاحكام من 87% إلى 98.4%. تحكم قوى تم تطوير ه للتحكم في المخمد MR لاجل الأطراف الصناعية. في هذا البحث، التطبيقات الأطراف الصناعية يكيف وعكس نموزج المخمد MR. ونتيجة تصميم وحدة التحكم مقارنة بالسلوك المستهدف تصل  $H\infty$ إلى %92.51. ويفترض أن أداء المحاكاة مقبول الأنها تتبع تقريبًا بنمط التصميم المستهدف.

### **APPROVAL PAGE**

I certify that I have supervised and read this study and that in my opinion, it confirms to acceptable standards of scholarly presentation and is fully adequate, in scope and quality, as a thesis for the degree of Master of Science (Mechatronics Engineering).

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## DECLARATION

I hereby declare that this thesis is the result of my own investigations, except where otherwise stated. I also declare that it has not been previously or concurrently submitted as a whole for any other degrees at IIUM or other institutions.

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# LIST OF SYMBOLS

| $\eta_P$          | Plastic Viscosity              |
|-------------------|--------------------------------|
| τ                 | Shear Stress                   |
| γ                 | Shear Strain                   |
| Ϋ́                | Shear Rate                     |
| $	au_y$           | Yield Stress                   |
| Н                 | Magnetic Field Strength (A/m)  |
| М                 | Magnetization (A/m)            |
| С                 | Curie Constant of Material (K) |
| Т                 | Temperature (K)                |
| $f_c$             | Frictional Force               |
| fo                | Offset Force                   |
| C0, C1            | Damping Coefficient            |
| F                 | Damping Force                  |
| $k_{0,} k_{1}$    | Spring Stiffness               |
| X0                | Initial Deflection             |
| α                 | Scaling Factor                 |
| z, Α, β, γ, n, δ  | Hysteretic Parameters          |
| $A_m$             | Amplitude                      |
| f                 | Frequency (Hz)                 |
| t                 | Time (s)                       |
| i                 | Current (A)                    |
| $m_b$             | Mass of Body                   |
| $S_W$             | Horizontal Walking Speed       |
| $W_g$             | Weight of Body                 |
| $L_c$             | Walking Stride Length          |
| $t_c$             | Contact Time                   |
| ta                | Aerial Time                    |
| t <sub>step</sub> | Time Step                      |

## LIST OF ABBREVIATIONS

- SACH Solid Ankle Cushioned Heel
- ESAR Energy Storage and Return
- IP Intelligent Prosthesis
- MR Magnetorheological fluid
- UTM Universal Testing Machine
- GA Genetic Algorithm
- FLS Fuzzy Logic System
- ANN Artificial Neural Network
- IPGA Intergeneration Projection Genetic Algorithm
- NGSA II Non-dominated Sorting Genetic Algorithm II
- PSO Particle Swarm Optimization
- PID Proportional-Integral-Derivative
- LQG Linear Quadratic Gaussian
- LQR Linear Quadratic Regulator
- $H_{\infty}$  H-infinity
- FTM Fatigue Testing Machine
- LVDT Linear Variable Differential Transformer
- GRF Ground Reaction Force

# CHAPTER ONE INTRODUCTION

#### **1.1 BACKGROUND OF THE STUDY**

Daily human activities are mostly required for humans to mobilize from a place to another. Walking and running are the methods of human locomotion, using two legs as support and propulsion to move around. However, for amputees, especially transtibial (below-knee) amputees require prosthesis to support them in walking and improving their gait.

A lot of research on designing and improving the performance of transtibial prosthetic limbs has done over a decade. The most common available transtibial prosthetic limbs are Solid Ankle Cushioned Heel (SACH) at which, the walking shock absorption comes from the cushioned heel. However, the ability of SACH to absorb the shock or damping forces is limited. Energy Storage and Return (ESAR) foot is another option, where it can absorb a significant amount of shock or damping forces during the loading phase and release it later during push-off (Grimmer et al., 2016). Nevertheless, both devices are passive, in which unable to provide mechanized energy or positive power to adjust the amputee's gait cycle and help them to propel forward (Lemoyne, 2016).

Active transtibial prosthetic limbs contain powered element to support in locomotion for the whole gait cycle (Hitt, Sugar, Holgate, & Bellman, 2010). Power Knee by Össur, Intelligent Prosthesis (IP) by Blatchford, Intelligent Knee by Nabtesco and C-Leg by Otto Bock are the examples of available powered actuated prosthetic limbs (Grimmer et al., 2016). These devices are actuated using either DC motor, pneumatic, or hydraulic actuators. Power Knee, for example, provides maximum support at knee joint for active bending (flexion) and extension during walking, helping amputees to go further. Apart from that, Grimmer et al. (2016) proposed an improved version of the active prosthetic ankle by Markowitz et al. (2011) to mimic the behaviour of human ankle movement. This device emphasizes dorsiflexion and plantarflexion control to adapt to terrain variation and walking speed. Even though active prosthesis can support amputees for the whole gait cycle and provide positive power e.g., climbing stairs, more energy is required since they are continuously active (Lui, Awad, Abouhossein, Dehghani-Sanij, & Messenger, 2015). Figure 1.1 shows the example of available passive and active transtibial prosthetic limbs.



Figure 1.1 Passive transtibial prosthetic limbs (ESAR) (left side) and active transtibial prosthetic limbs (right side) (retrieved from "Feet and Ankles", 2018).

Before design the transtibial prosthetic limbs, the basic gait cycle is discussed. It is owing to understand the gait cycle help to better detect the critical phase that acquired much more attention in designing the prosthesis. Gait is known as a manner of walking, and the gait cycle defined as the period of repetitive events of walking. The single gait cycle is measured where one foot contacts the ground until the same foot touches the ground again in locomotion. The gait cycle is divided into two main phases: the stance phase and the swing phase, as shown in Figure 1.2. Generally, the stance phase occupies approximately 60% of the single gait cycle and 40% by swing phase. However, this varies with walking speed, where the swing phase will be more prolonged, and the stance phase will be shorter when the rate increased (Whittle, 2007).



Figure 1.2 Positions of legs during single gait cycle (blue) (Pirker & Katzenschlager, 2016).

A detail of the gait cycle for stance phase recognizes five significant events which are:

- 1) Heel strike
- 2) Loading response,
- 3) Mid-stance,
- 4) Terminal stance, and
- 5) Pre-swing.

While the swing phase divided into three significant events which are:

- 1) Toe-off or initial swing,
- 2) Mid-swing, and
- 3) Terminal swing (J. Park, Yoon, Kang, & Choi, 2016).

At the beginning of a stance phase, a transient force known as a heel strike is generated. The heel strike transient represents an exchange of momentum when the foot contacts the ground, terminating the previous movement (Addison & Lieberman, 2015;

Tongen & Wunderlich, 2012; Zinner & Sperlich, 2016). Figure 1.3 shows the ground reaction force in the vertical direction from a walk experimented by Whittle (2007). The heel strike transient happens typically at 10 ms to 20 ms and is seen as a short spike of force.



Figure 1.3 Plot of vertical ground reaction force (N) against time (ms) (Whittle, 2007).

It has been found that the resulting shock wave from the heel strike may produce damage to the human body. The previous researchers suggested there are possible shock-related injuries due to the heel strike transient, including headaches and osteoarthritis (degenerative joint disease) (Light, McLellan, & Klenerman, 1980), stress fractures (Dickinson, Cook, & Leinhardt, 1985), plantar fasciitis (D. Singh, Angel, Bentley, & Trevino, 1997), chronic low back pain, degeneration of cartilage (C. Y. Lin, Chuang, & Cortes, 2017) and prosthetic joint loosening (Whittle, 2007).

Possible solutions to reduce the effect of heel strike transient, especially prosthetic limb users, is the use of a heel pad (Jorgensen & Ekstrand, 1988). This is the earliest solution to encounter the heel strike, yet it only able to absorb the transient force approximately up to 47 to 66% (Whittle, 2007). The control of plantar flexion of ankle

and knee is another possible solution where it presumes to provide shock absorption immediately after initial contact (Ebbeling, Hamill, & Crussemeyer, 1994). However, plantar flexion of ankle and knee occupies at 80 ms and 150 ms respectively slower than heel strike transient (20 ms), thus impossible to protect the leg from the transient force (Whittle, 2007).

Hence, to provide a better solution for the need for shock absorption for transtibial amputees, a device that is damper-based shock absorber is suggested. A semi-active damper is adopted in the design of the prosthetic limb to capture the advantages of passive damper, along with performing as good as an active damper. The design also will mainly focus on reducing the heel strike transient effect. This research describes the use of a Magnetorheological damper or MR damper (semi-active damper) in the transtibial prosthetic limb. The work is initiated with understanding the parameters that affect the performance of MR damper. A controller is then designed so that the system is capable of reducing vibrations at various walking speeds.

#### **1.2 PROBLEM STATEMENT**

When human in motions either walking or running, human lower limb's damping characteristic changes to provide proper movement condition. However, uncontrolled exposure to vibration especially during heel strike may lead to injuries or prosthesis malfunction. Having an adaptive capability in artificial prosthesis for lower limb amputees is necessary to provide essential movements and attenuate unwanted vibration. To design an adaptive prosthetic limbs, a semi-active damping device which is Magnetorheological Fluid (MR) damper is proposed. This device have the capabilities to attenuate broadband vibration without consuming much power consumption.

However, major drawbacks that restrict the applications of MR damper are nonlinear hysteresis force-velocity and force-displacement characteristic. Thus, to design high efficiencies of MR damper applications, an accurate mathematical model that can take full advantages of this device is required. Developing and utilizing these devices become more challenging due to inherent nonlinear nature of the dampers. In this study, the dynamic response of the MR damper is investigated by testing the damper under different conditions. Then, the dynamic models of the damper is developed using a proposed method. The proposed method will help for further research as reference on how to estimate the dynamic models. For further investigation, the proposed dynamic models are expected to be applied on practical applications, prosthetic limb for example. On these bases, semi-active controller system, consist of a system controller and a damper controller are required. System controller is to generate desired force based on dynamic response of a plant while the damper controller is to track the generated damping force by adjusting the value of voltage or current. The inverse dynamic model of the damper is required to design the damper controller. The detail of the design will be explained in the next chapter.

#### **1.3 RESEARCH OBJECTIVES**

The objectives of this research are:

- 1. To understand the behavior of MR damper under various input current and damping frequency.
- 2. To estimate and optimize the parameters of the MR damper models based on experimental result.
- 3. To control the MR damper for transtibial prosthetic limb application.

#### **1.4 RESEARCH METHODOLOGY**

The methodology to achieve the research objectives is adopted as follows (flow chart of research methodology may refer to Figure 1.4):

 a) Exploring the MR damper background and analyzing its problems through an extensive literature review

Carry out an extensive study of the published works to fully comprehend and value the significance, scope, and underpinnings of this research. The outcome of this study should be the identification of critical parameters or factors to improve the dynamic range of MR damper.

b) Experimental investigation

Carry out an experimental study to test the MR damper's dynamic behavior under the variation of parameters. The force-displacement and force-velocity relationship are the expected outcome of the test.

c) Parametric optimization of MR damper model

Identify the available MR damper model and perform parametric optimization on the model by comparing with the experimental result. The outcome of the task is to have a mathematical model in which able to describe the actual performance of MR damper.

d) Controller design

Design controller to control MR damper for prosthetic limb application. The expected outcome from the task is to have a robust control algorithm to control the prosthetic limb and a controller (inverse MR damper model) to control the MR damper.